

# Chaos Function Based - Secure Deniable Authentication Protocol

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**Abstract - Deniability is defined as a privacy property which enables protocol principals to deny their involvement after they had taken part in a particular protocol run. This paper demonstrates that Yoon & Yoo's scheme is insecure to a Key-Compromise Impersonation (KCI) attack and Replay attack. Based on this, propose an Enhanced Scheme which preserves the authenticity, deniability and resistance against the KCI attack using Chaos function  $f(x) = 4 * x * (1-x)$  and Replay attack using Timestamp. This paper demonstrates that Yoon and Yoo's scheme "Secure Deniable Authentication Protocol Based on ElGamal Cryptography" is susceptible to KCI attack and replay attack. To mitigate this security breach, propose an improved deniable authentication protocol based on Chaos Function and ElGamal Cryptography. future work is to extend this proposed Deniable Authentication Protocol for Micro Payment and Macro Payment in E-Commerce applications.**

**Keyword: Deniable, Authentication, ElGamal Cryptography, Chaos Function, KCI attack.**

## I. INTRODUCTION

The Deniable Authentication Protocol [1, 4, 5, 7-9] is a new technique of modern cryptography, compared with traditional authentication, it has two characteristics; first, a receiver can verify the source of the message as in the traditional authentication protocol. Second, a receiver cannot prove the source of the message to a third party. In 2005, Wang et al. [8] proposed an efficient deniable authentication protocol (WLT), which makes use of the inverse of the ElGamal cryptosystem. It requires less computational complexity and communication cost. In 2006, Shao et al. [7] however, pointed out that the WLT protocol is insecure to a person-in-the-middle attack. That is in the whole process, the receiver cannot be aware of the existence of the adversary as well as the modification of the messages. They have also proposed an improved deniable authentication protocol (SCL) based on ElGamal cryptography [3]. In 2008 Yoon and Yoo [9] pointed out that Shao et al.[7] scheme still suffers from person-in-the-middle attack. They proposed one secure deniable authentication protocol based on ElGamal cryptography [3]. However, this paper points out that all the above schemes suffer from Key-Compromise Impersonation (KCI) attack [5] and replay attack. Once if the long-term secret key of any user is compromised, the

total security of the communication will be compromised. Deniable Authentication Protocol is used under certain circumstances such as electronic voting system, online shopping and negotiation over the internet. In these systems, security of communication plays a major role. In a distributed environment denial of service (DOS) attack is the most common one. Replay attack is one kind of DOS attack. In improved protocol achieve the resistance to KCI attack by using chaos function. An algorithm using one of the simplest chaotic function [6]  $f(x) = 4 * x * (1-x)$  is used.

## II. RELATED WORK

In the past several years, numerous deniable authentication protocols have been proposed but many of them have also been proven to be vulnerable to various cryptanalytic attacks [15-17]. The concept of deniable authentication protocol was initially introduced by Dwork et al. [18], which is based on the concurrent zero knowledge proof. However, this scheme requires a timing constraint. Not only that, the proof of knowledge is also time-consuming [1]. Another notable scheme which was developed by Aumann and Rabin [11, 12] is based on the intractability of the factoring problem, in which a set of public data is needed to authenticate one bit of a given message. Few years later, Deng et al. [1] have proposed two deniable authentication schemes based on Aumann and Rabin's scheme. The proposed schemes are based on the intractability of the factoring problem and the logarithm problem. However, in 2006, Zhu et al. [17] have successfully demonstrated the Man-in-the-Middle attack against Aumann and Rabin's scheme and this indirectly results in an insecure implementation of Deng et al., schemes. In 2003, Boyd and Mao [13] have proposed another deniable authenticated key establishment for Internet protocols based on elliptic curve cryptography. These schemes are believed to be able to solve the complexity of computation and appear to be more efficient than others but their vulnerability to KCI attack has been exploited by Chou et al. [ ] in 2005. Besides that, Fan et al. [4] have proposed a simple deniable authentication protocol based on Diffie-Hellman key distribution protocol in 2002. Unfortunately, in 2005, Yoon et al. [16] have pointed out that their protocol suffers from the intruder

masquerading attack and subsequently proposed their enhanced deniable authentication protocol based on Fan et al.'s scheme.

In addition, in 2005, Cao et al. [14] have proposed an efficient ID-based deniable authentication protocol which enables a dynamic shared secret to be derived as a session key. Unfortunately, in 2006, Yoon et al.'s enhanced scheme and Cao et al.'s scheme are proven to be impractical and susceptible to KCI attack respectively by Chou et al. [15]. Moreover, Chou et al. have proposed another new deniable authentication protocol [15] and they have claimed that their proposed protocol has achieved strong deniability as well as authenticity with great resistance against KCI attack. In 2007, Meng-Hui Lim et al. [5] have proved that Chou et al.'s scheme provides inadequate resistance against KCI attack. In 2008, Eun-Jun Yoon et al. [9] has proposed one deniable authentication protocol which is based on Elgamal Cryptography.

### III. KCI ATTACK ON YOON AND YOO'S SCHEME

The list of terms and their definitions used in Yoon and Yoo's scheme [9] and scheme are given in Table 1.

TABLE 1

Terms	Meanings
S	Sender
R	Receiver
p	Prime Number
g	Primitive Root
$x_s$	Sender's private key
$y_s$	Sender's Public key
$x_r$	Receiver's private key
$y_r$	Receiver's Public key
DH	Shared key
a	Random number $a \in Z_p$
H()	One way hash function
	Concatenation Symbol
M	Message to send
$rk_i$	Random session key generated by chaotic function
T	Timestamp

In this section, will depict how Yoon and Yoo's [9] scheme can be intruded by KCI attack. In fact, this attack is deemed successful only if the adversary manages to masquerade as another protocol principal to communicate with the victim after the victim's private key has been compromised. Assume that an adversary E, has the knowledge of sender's private key  $x_s$  and he intends to launch the KCI attack against sender by pretending receiver to communicate with sender.

**Step 1:** Adversary E chooses a random number  $a'$  and computes DH by using the equation  $DH = y_r^{x_s} \bmod p$  and  $A'$  and  $C1'$ . Then, he initiates the communication by sending  $A'$  and  $C1'$ .

**Step 2:** After receiving  $A'$ ,  $C1'$ , sender thought that receiver is trying to communicate with him. He verifies the received value from receiver, if the verification is successful, sender truly believes that he is communicating with receiver although he is in fact communicating with adversary E. Hence, KCI attack is successful.

**Step 3:** Sender chooses the message M and it computes  $C2$  and  $C3$ .

As we know that, Deniable Authentication Protocol is used in sensitive area like Electronic Voting System, Online shopping, negotiation over the Internet in which security of communication is more important. But demonstrated that Yoon and Yoo's Scheme is insecure against KCI attack.

### IV. ENHANCED SCHEME

As we have noticed in the previous section, Yoon and Yoo's [9] Scheme has fallen into the KCI attack mainly due to their failure in concealing the value of  $C1$  and  $C2$  when  $x_s$  ( $x_r$ ) is exposed. Once the adversary has obtained  $x_s$  ( $x_r$ ), he is able to derive all the subsequent parameters as well as the message. In other words, the values of  $C1$  and  $C2$  should be obscured even if  $x_s$  or  $x_r$  has been compromised so as to resist the KCI attack. For this purpose, we use a Chaotic function [6]  $f(x) = 4 * x * (1-x)$  for calculating the random key and communicate Chaotic function and their parameters through telephone and other parameters through network. So, our assumption is Intruder have no idea to tap the message through network and telephone lines at the same time. Partial listening (tapping) of information either through telephone or network should not allow the Adversary to launch the KCI attack.

#### A. Chaos Function

Chaotic functions [6] which were first studied in the 1960's show numerous interesting properties. The iterative values generated from such functions are completely random in nature although limited by certain bounds. However, the most fascinating aspect of these functions is their extreme sensitivity to initial condition. A slight difference in the Initial Starting value i.e.,  $i_0$  leads to substantial difference in the obtained iterative values. This is tabulated in Table 2.

TABLE 2

Error in the Starting Value	Iteration number after which the difference in values > 0.0625
1 E -02	5

1 E-05	14
1 E-10	26
1 E-16	49

The divergence of obtained Chaos values for  $i_0$  a small disturbance in initial starting value can be seen much more clearly in Figure 1.

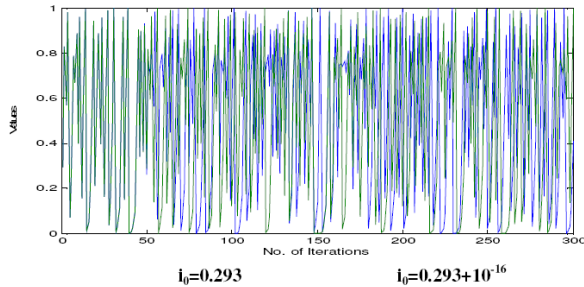


Figure 1: Iterative values obtained for two different starts

1. Generating Values from Chaos Function

The chaotic function which have considered is  $f(x) = 4 * x * (1-x)$ . To generate the values from this chaotic function the following three factors have to be first decided.

1. The starting value for the iteration ( $i_0$ ).
2. The number of iterations after which the first value can be picked for generating keys.
3. The number of iterations to be maintained beten 2 picked values thereafter.

For example,  
 Start Value – 0.293  
 First iteration to be considered – 119  
 Number of iterations for separation – 27  
 This will provide the set of values.

2. Generation of random session key from chaotic values

It is proposed that the values yielded by the Chaos function are converted to Binary fractions whose first 16 bits are taken and their decimal equivalent will be ed as the random session key.

$$rk_i = (b_0-b_{15} \text{ of chaotic values})_{10} \quad 1 \leq i < n.$$

B. Proposed Deniable Authentication Protocol

This section proposes an improved Deniable Authentication Protocol to solve the security problems mentioned in Section 3. There are f steps in the proposed protocol as follows.

**Step 1:** The Receiver R first computes Diffie-Hellman value  $DH = y_s^{x_r} \text{ mod } p$  by ing Sender’s Public key  $y_s$  and his/her own private key  $x_r$ . Then R chooses a Random number

$a \in Z_p^*$  and computes  $A = g^a \text{ mod } p$  and  $C1 = H(A || DH || rk)$ , and finally sends A and C1 to the Sender S while keeping ‘a’ secret.

**Step 2:** After receiving A and C1 from R, S computes Diffie-Hellman value  $DH = y_r^{x_s} \text{ mod } p$  by ing Receiver’s Public key  $y_r$  and his/her own private key  $x_s$ . S checks

$$C1 = H(A || DH || rk).$$

If this equation holds, then S authenticates R; otherwise, values are rejected. When S wants to send a message M to R, he/she computes  $C2 = A^{x_s} M. rk \text{ mod } p$ ,  $C4 = H(rk || T)$  and  $C3 = H(M || rk)$ .

S finally sends (C2, C3, C4, T) to R. Further communications will be continued by varying timestamp alone without varying random key in order to reduce the computational complexity.

**Step 3:** R first checks  $C4 = H(rk || T)$ . If this equation holds, step 4 will be processed. Otherwise request is rejected.

**Step 4:** R gets the message M by  $M = C2 \text{ mod } p$  and checks  $C3 = H(M || rk)$ . If this equation holds, then R accepts the message M; otherwise message is rejected.

V. PROPOSED PROTOCOL

Security Analysis

In this section, will scrutinize enhanced DAP ing Chaos function in order to ensure that the security requirements for a Deniable Authentication Protocol are satisfied.

Lemma 1: Enhanced Protocol is Deniable

Proof: Once (C2, C3, C4) is received and verified, Receiver can easily identify the sce of the message M, since the message is integrated with Sender’s private key and random key. After verification Receiver R can be assured that the message originated from Sender S. If receiver R intends to expose the message Sender’s identity to a third party, Sender S would be able to repudiate as he/she would argue that receiver R could also generate (C2, C3, C4) by ing Sender’s public key, random number and random key. Hence the deniability property is satisfied.

Lemma 2: The proposed protocol provides Mutual Authentication

Proof: In Step 2, Sender S checks  $C1 = H(A || DH || rk)$  to authenticate the Receiver R. In Step 3, the Receiver R also checks  $C4 = H(rk || T)$  to authenticate the Sender S.

*Lemma 3: The enhanced protocol is able to resist the KCI attack.*

Proof: The resistance of the enhanced protocol towards KCI attack is analyzed by considering the following 2 scenarios.

a. Receiver's Private Key  $x_r$ , has been compromised.

Initially, the Receiver R (Adversary E) chooses a random number  $a'$ , computes  $A'$  and computes  $C1' = H(A' || DH || rk')$  and sends it to Sender S. ?

Sender S first checks  $C1=H(A' || DH || rk)$ . If this equation does not hold, Sender S terminates the session.

b. Sender's Private Key  $x_s$ , has been compromised.

Initially, the Receiver R chooses a random number  $a$ , computes  $A$  and  $C1 = H(A || DH || rk)$  and sends it to S. Adversary (E) intercepts (A, C1) and he omits the C1 computation. He is not able to compute C1 and checks the received value, because he doesn't know the  $rk$  value. Adversary E chooses a Message  $M'$  and a random key  $rk'$  and computes  $C2'$ ,  $C4'$  and  $C3'$  as follows.

$$\begin{aligned} C2' &= A^{x_s} \cdot M \cdot rk' \pmod p \\ C4' &= H(rk' || T) \\ C3' &= H(M' || rk') \end{aligned}$$

Receiver R checks the  $C4$  value. If it is invalid, Receiver R confirms that there is an intruder and terminates further communication.

*Lemma 4: The enhanced protocol is able to resist the Replay attack.*

Proof: In the proposed protocol, Time stamp  $T$  and Random Key  $rk$  is included in constructing the parameter  $C4$  and sends the quadruple( $C2, C3, C4, T$ ) to Receiver R. R first computes  $C4$  value. If it is invalid, R rejects the message. By this way replay attack is avoided.

*Lemma 5: The enhanced protocol withstands the Person-in-the Middle attack.*

Proof: In the Proposed protocol to do a Person-in-the Middle attack, Adversary  $mt$  impersonate like  $S$  with  $R$  and  $R$  with  $S$ . For this purpose the attacker is required to know  $A_x$  or  $y_s$  and  $rk$ . This is equivalent to solving discrete logarithmic problem and solving chaos function. Therefore the proposed protocol withstands the Person-in-the Middle attack.

## VI. CONCLUSION AND FUTURE WORK

This paper demonstrates that Yoon and Yoo's scheme "Secure Deniable Authentication Protocol Based on ElGamal Cryptography" is susceptible to KCI attack and replay attack. To mitigate this security breach, propose an improved deniable authentication protocol based on

Chaos Function and ElGamal Cryptography. future work is to enhance this proposed Deniable Authentication Protocol for Micro Payment and Macro Payment in E-Commerce applications.

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